Exam Code:211002

Bubject Code: 4979

M.Sc. (Mathematics) - 2nd Semester (2721)

Paper: MATH-565

Partial Differential Equations and Integral Equations

Time Allowed: 2 hrs.

Max. Marks: 100

Note: There are EIGHT questions of equal marks. Candidates are required to attempt any FOUR questions.

- (a) Find the integral surface of the linear PDE $x(y^2 + z)p y(x^2 + z)q = (x^2 y^2)z$ which contains the straight line x + y = 0, z = 1
 - (b) Find a complete integral of $p : (z + qv)^2$ using Charpit's method
- (a) By Jacobi's method, solve the equation $xp + 3yq = 2(z x^2q^2)$
 - (b) Find the surface which is orthogonal to the one -parameter system $z = exp(x^2 + y^2)$ and which passes through the hyperbola $x^2 - y^2 = a^2$, z = 0

Section - B

- 3. (a) By Monge's method, solve the PDE $3r + 4s + t + (rt s^2) = 1$
 - (b) Obtain the solution, valid when $x, y \ge 0$, $xy \ge 1$, of the differential equation $\frac{\partial^2 z}{\partial y \partial y} = \frac{1}{x+1}$ such that z = 0, p = 2y / (x + y) on the hyperbola xy = 1 https://www.gnduonline.com
- 4 Solve the wave equation $\frac{\partial^2 u}{\partial x^2} = \frac{\partial^2 u}{\partial x^2}$, 0 < x < 1, t > 0 subject to the conditions u(0,t) = u(1,t) = 0. u(x,0)=0 and $\frac{\partial u(0,t)}{\partial t}=1$

Section - C

- Solve the Volterra integral equation $y(x) = \frac{1}{1 + x^2} \int_0^x \frac{t}{1 + x^2} y(t) dt$
- Using the method of successive approximations, solve the Volterra integral equation

$$y(x) = 1 + x - \int_{0}^{x} y(t) dt, y_0(x) = 1$$

- Solve the Fredholm's integral equation $y(x) = \cos x + \lambda \int_{0}^{\infty} \sin(x-t)y(t)dt$
- Solve the Fredholm's integral equation, using the method of successive approximations,

$$y(x) = (x+1)^2 + \int_{-1}^{1} (xt + x^2t^2)y(t)dt$$
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