

B.A./B.Sc. 5th Semester

MATHEMATICS

Paper—I (Dynamics)

Time Allowed—3 Hours] [Maximum Marks—50

Note :— Attempt *five* questions in all selecting at least *two* from each section.

SECTION—A

1. (a) A point moving with uniform acceleration in a straight line describes equal distances in time

$$t_1, t_2, t_3; \text{ show that } \frac{1}{t_1} + \frac{1}{t_2} + \frac{1}{t_3} = \frac{3}{t_1 + t_2 + t_3}.$$

- (b) A, B, C are three points vertically below the point O such that OA = AB = BC. If the particle falls from rest at O, prove that the times of describing OA, AB and BC are as $1 : (\sqrt{2} - 1) : (\sqrt{3} - \sqrt{2})$. 5,5

2. Masses P and Q in a Atwood's machine are allowed to move from rest any distance x. If P is greater than Q, show that the mass which must suddenly be removed from P at the end of distance x, so that the motion in the same sense may continue a further distance nx, is

$$\frac{(n+1)(P^2 - Q^2)}{(n+1)P + (n-1)Q} \quad 10$$

3. (a) Two masses m_1, m_2 are connected by an inelastic string; m_2 is placed on a smooth horizontal table and the string passes over a light smooth pulley at the edge of the table and m_1 is hanging freely. Determine the motion and the tension in the string. Find also the pressure on the pulley.
- (b) A body sliding down a smooth inclined plane is observed to cover equal distances, each equal to l , in consecutive intervals of time t_1 and t_2 . Show that inclination of the plane is

$$\sin^{-1} \left[\frac{2l(t_1 - t_2)}{gt_1 t_2 (t_1 + t_2)} \right]. \quad 5,5$$

4. (a) A particle starts from rest and moves along a straight line with an acceleration f varying as t^n . If v be the velocity at a distance s from the starting point, show that $(n+1)v^2 = (n+2)fs$.
- (b) A particle free to move along the x-axis is subjected to a force $mF_0 \cos pt$ acting along x-axis. At $t = 0, x = 0$ and $v = 0$. Show that at any time

$$t, x = \frac{F_0}{p^2} (1 - \cos pt). \text{ Here } m \text{ is the mass of the particle. } F_0 \text{ and } p \text{ are constants. } 5,5$$

5. A particle is performing simple harmonic motion of period T about a centre O and it passes through the position P ($OP = b$) with velocity v in the direction OP. Prove that the time which elapses before it comes

$$\text{to P is } \frac{T}{\pi} \tan^{-1} \frac{vT}{2\pi b}. \quad 10$$

SECTION—B

6. (a) A particle is projected with velocity u so that its range on a horizontal plane is twice the greatest height attained. Show that range is $\frac{4u^2}{5g}$.

(b) The maximum height of a projectile is h and angle of projection is α . Find out the difference of time when it is at height of $h \sin^2 \alpha$. 5,5

7. A particle is projected from O at an elevation α and after time t , the particle is at P . Prove that $\tan \beta = \frac{1}{2} (\tan \alpha + \tan \theta)$ where β and θ are respectively the inclinations to the horizontal of OP and of the direction of motion of the particle when at P . 10

8. (a) A train of mass M kg is ascending a smooth incline of 1 in n and when the velocity of the train is vm/sec , its acceleration is $f \text{ m/sec}^2$. Prove that the effective power of the engine is $\frac{Mv(nf + g)}{n}$ watts. <http://www.gnduonline.com>

(b) Prove that the kinetic energy of a particle of mass m moving with a magnitude of velocity v is $\frac{1}{2} mv^2$. 5,5

9. A particle of mass m is tied to the middle point of an elastic string of natural length $2l$ and modulus λ . The ends of the string are tied to two points on a smooth horizontal table distant $2L$ ($L > l$). Find the period of small oscillation (i) along the string (ii) perpendicular to the string. 10

10. A pendulum of length l hangs against a wall inclined at an angle α to the horizontal. Show that the time of complete oscillation is $2\pi \sqrt{\frac{l}{g \sin \alpha}}$. 10

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